



Running the Statistical Gauntlet in R



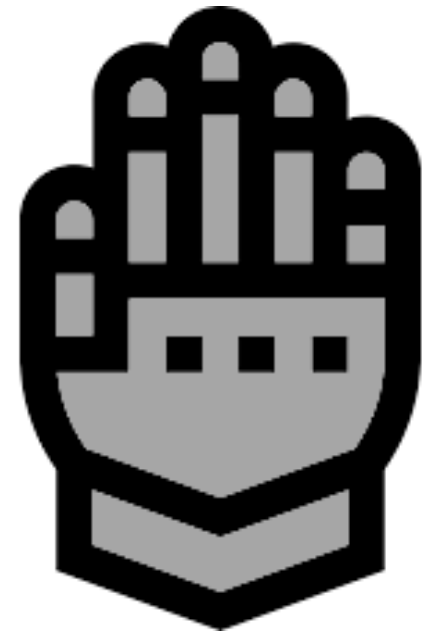
Dr. Mark Williamson, PhD

Biostatistics, Epidemiology, and Research Design Core

DaCCoTA, University of North Dakota

Introduction

- ❖ Common for introductory statistics courses to use only one or two examples to explain a model or method
- ❖ Makes it difficult to adapt that example's particularities to your own work
- ❖ Also fails to train your eye in reading and understanding patterns across examples
- ❖ Here, we aim to remedy that by providing exhaustive, back-to-back examples
- ❖ Aimed at introductory to intermediate learners



Overview

- ❖ Today, we'll be using R
 - ❖ Access R software via <https://cran.r-project.org/>
 - ❖ Access R Studio software via <https://rstudio.com/>
 - ❖ Access R code at: https://med.und.edu/daccota/files/docs/berdc_docs/model_gauntlet_rcode.txt
- ❖ All datasets used are available in R via packages or weblink
- ❖ Topics Covered
 - T-tests
 - 1) One-sample t-test
 - 2) Two-sample t-test
 - 3) Paired t-test
 - ANOVA
 - 4) One-way ANOVA
 - 5) Two-way ANOVA
 - 6) Blocked/Nested ANOVA
 - Regression
 - 7) Simple Linear Regression
 - 8) Multiple Linear Regression
 - 9) Logistic Regression



Procedure

- ❖ Six examples per topic
- ❖ The **test statistic**, **p-value**, and where appropriate, **model fit** will be outlined by color
- ❖ Each example includes:
 - Research question in the form of a sentence
 - Relevant statistical results from R
 - most values will be rounded to two decimal places
 - p-values will not be modified
 - Written answer to research question
 - Figure or table when appropriate
 - Some graphs will be of null results for clarity (greyscale or red)
 - Typically, only significant results are graphed
- ❖ Get ready to run the gauntlet!





One-sample t-test

❖ *Tests if a variable's mean is different from a set value*

#1) Is the average miles per gallon (mpg) of 1975 Motor Trend vehicles less than 25?

$t = -4.61$, $df = 31$, $p\text{-value} = 3.293e-05$
95 percent confidence interval: -Inf 21.90
mean of x: 20.09

Yes, MPG is less than 25.

#2) Is the average quarter mile time in seconds (qsec) of 1975 Motor Trend vehicles greater than 17.5?

$t = 1.10$, $df = 31$, $p\text{-value} = 0.139$
95 percent confidence interval: 17.31 Inf
mean of x: 17.85

No, quarter mile time is not greater than 17.5

#3) Is the average weight in 1000 lbs (wt) of 1975 Motor Trend vehicles different than 3?

$t = 1.26$, $df = 31$, $p\text{-value} = 0.2185$
95 percent confidence interval: 2.86 3.57
mean of x: 3.22

No, weight is not different than 3.

#4) Is the log baseline number of seizures (lbase) for the placebo group of epileptics different than 0?

$t = -0.55$, $df = 111$, $p\text{-value} = 0.5849$
95 percent confidence interval: -0.190 0.11
mean of x: -0.04

No seizure number not different from 0.

#5) Is the average yield of barley for 1931 greater than 100?

$t = 1.73$, $df = 29$, $p\text{-value} = 0.04731$
95 percent confidence interval: 100.15 Inf
mean of x: 109.05

Yes, yield is greater than 100.

#6) Is the average yield of barely for 1932 different than 1931's (109)?

$t = -3.58$, $df = 29$, $p\text{-value} = 0.001235$
95 percent confidence interval: 84.07 102.20
mean of x: 93.13

Yes, yield is different than 109.

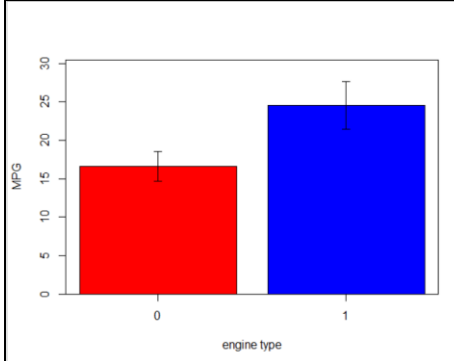


Two-sample t-test

❖ Tests if the means of two different groups are different

#1) Is the average miles per gallon (mpg) of 1975 Motor Trend vehicles different between v-shaped (0) and straight (1) engines (vs)?

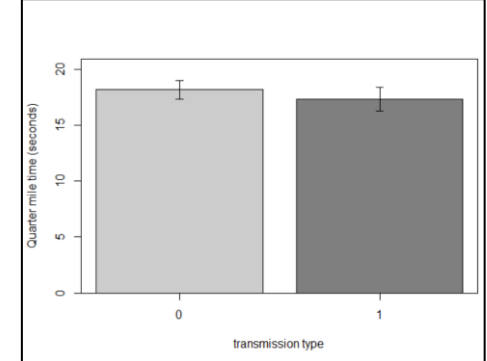
t = -4.67
p-value = 0.0001098
Group 0 mean = 16.62
Group 1 mean = 24.56



Yes, straight engines (1) had higher MPG than v-shaped ones (0).

#2) Is the average quarter mile time in seconds (qsec) of 1975 Motor Trend vehicles greater in automatic (0) compared to manual (1) transmissions (am)?

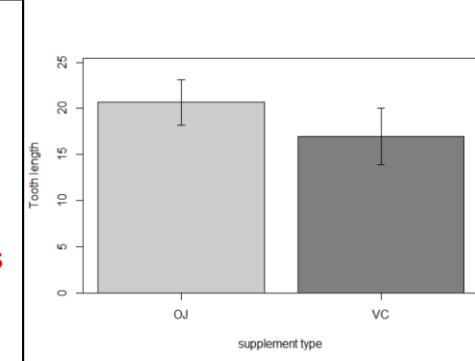
t = 1.29
p-value = 0.1047
Group 0 mean = 18.18
Group 1 mean = 17.36



No, automatic transmissions (0) did not have higher quarter mile times than manual (1).

#3) Is the average tooth length of guinea pigs (len) different between orange juice (OJ) and ascorbic acid (VC) supplement of vitamin C (supp)?

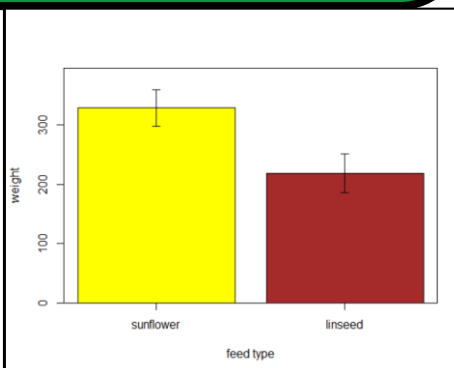
t = 1.92
p-value = 0.06063
OJ mean = 20.66
VC mean = 16.96



No, OJ and VC supplemented guinea pigs did not have different tooth lengths.

#4) Is the average weight (weight) lower in linseed fed chicks compared to sunflower fed ones (feed)?

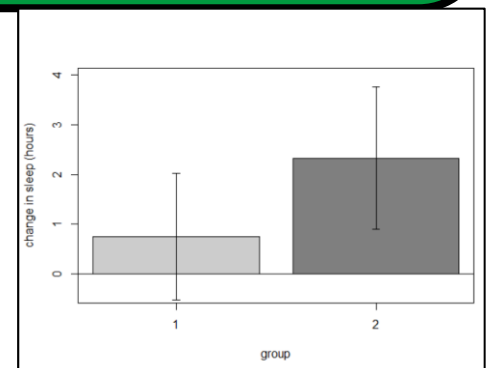
t = -5.34
p-value = 1.187e-05
Sunflower mean = 218.75
Linseed mean = 328.92



Yes, linseed-fed chicks had lower weight than sunflower-fed chicks.

#5) Is the change in hours of sleep (extra) different between two groups of students (group)?

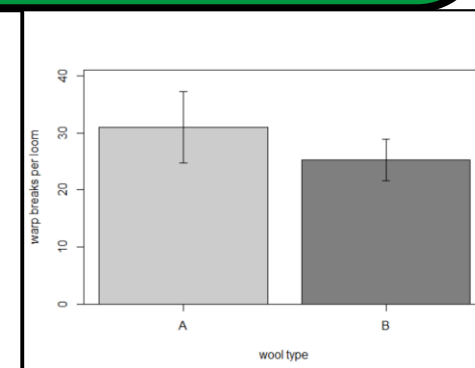
t = -1.86
p-value = 0.07939
Group 1 mean = 0.75
Group 2 mean = 2.33



No, group 1 and 2 did not have different changes in hours of sleep.

#6) Is the number of warp breaks per loom (breaks) different between two types of wool (wool)?

t = 1.63
p-value = 0.1098
Group A mean = 31.04
Group B mean = 25.26



No, type A and B wool did not have different number of warp breaks.

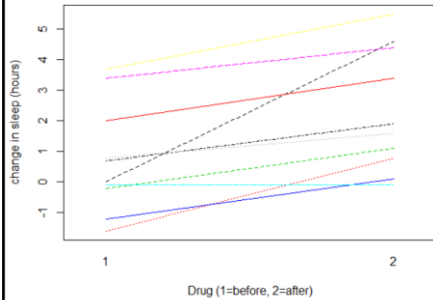


Paired t-test

❖ Tests if the means of two different paired groups are different

#1) Is the change in hours of sleep (extra) different between students before (1) and after (2) a drug (group)?

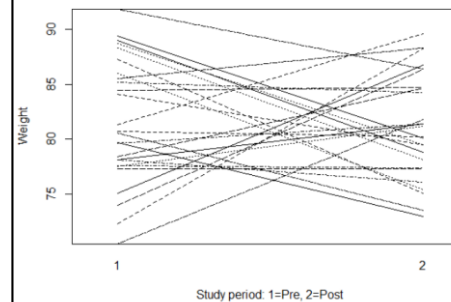
t = -4.06
p-value = 0.002833
Mean difference = -1.58



Yes, students had a higher change in sleep after the drug compared to before.

#2) Is the average weight (Weight) of anorexia females greater in the post study period compared to the pre study period (Period) for the Control group?

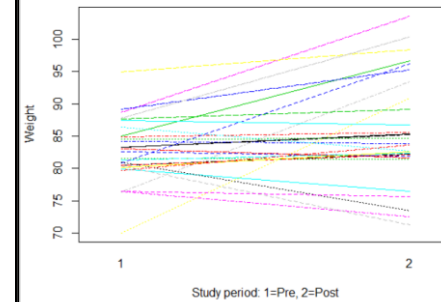
t = -0.29
p-value = 0.6118
Mean difference = -0.45



No, female weights were not higher in the post-study period compared to the pre-study period for the Control group.

#3) Is the average weight (Weight) of anorexia females greater in the post study period compared to the pre study period (Period) for the the Cognitive Behavioral Treatment group?

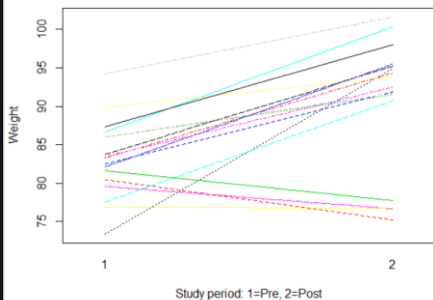
t = 2.22
p-value = 0.01751
Mean difference = 3.01



Yes, female weights were higher in the post-study period compared to the pre-study period for the CBT group.

#4) Is the average weight (Weight) of anorexia females greater in the post study period compared to the pre study period (Period) for the Family Treatment group?

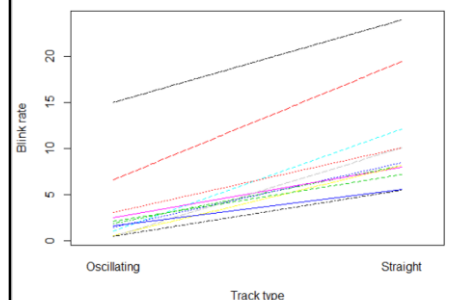
t = 4.1849
p-value = 0.0003501
Mean difference = 7.26



Yes, female weights were higher in the post-study period compared to the pre-study period for the FT group.

#5) Is the average blink rate (Rate) different between participants steering a pencil along a straight or oscillating track (Track)?

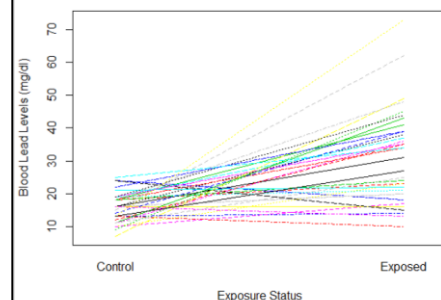
t = -9.74
p-value = 9.621e-07
Mean difference = -7.5



Yes, blink rates were higher in the straight track compared to the oscillating track.

#6) Is the average blood lead level (Levels) lower in control children compared to exposed children (Status)?

t = -5.78
p-value = 1.018e-06
Mean difference = -15.97



Yes, blood lead levels were lower in the control children compared to the exposed children.



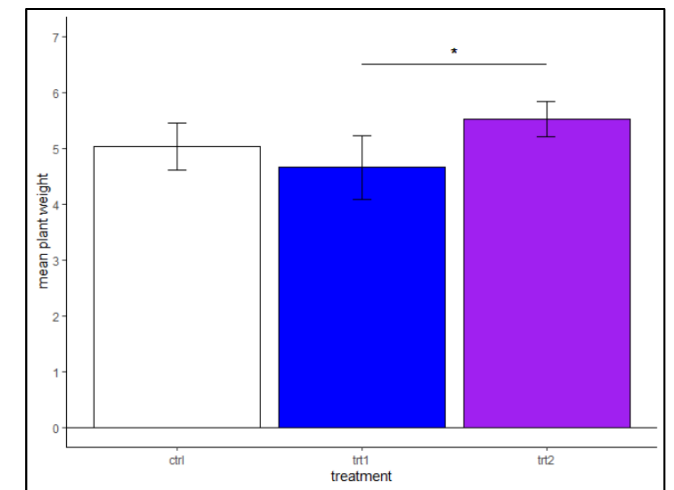
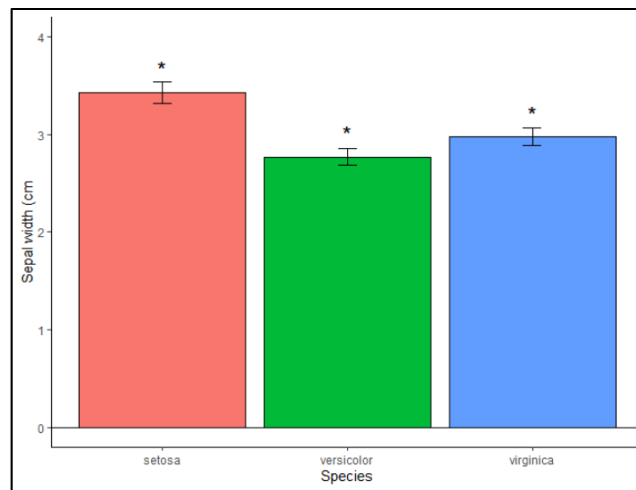
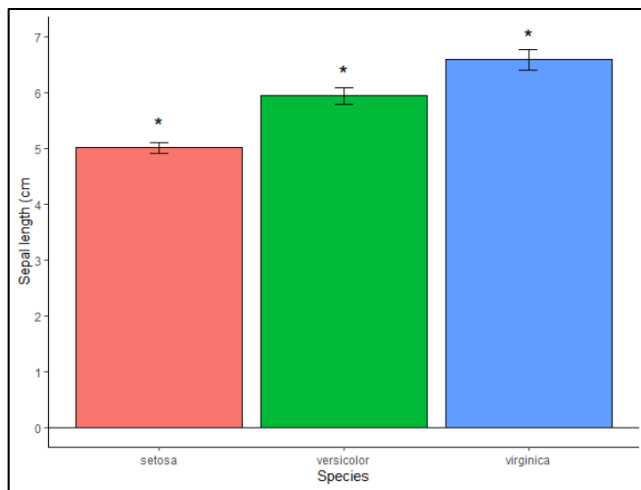
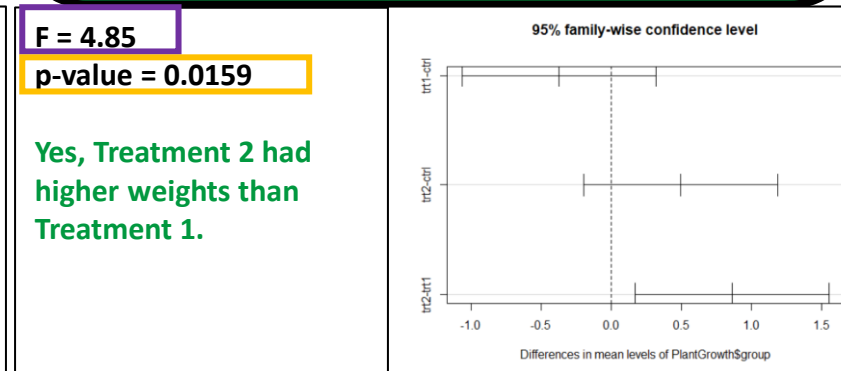
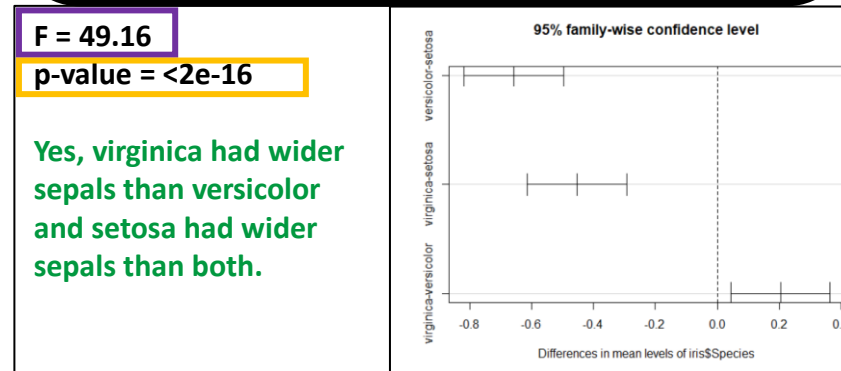
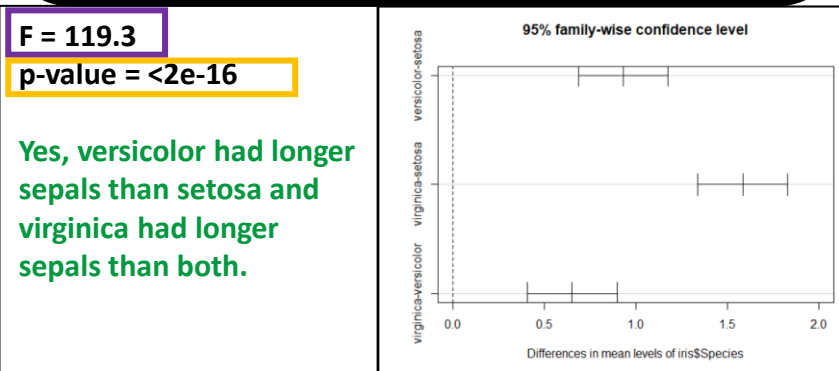
One-way ANOVA

❖ Tests if a variable's mean is different between a category with three or more groups

#1) Is the average sepal length different across three species of iris (Species)?

#2) Is the average sepal width different across three species of iris (Species)?

#3) Is the average plant growth (weight) different across treatments (group)?





One-way ANOVA cont.

❖ Tests if a variable's mean is different between a category with three or more groups

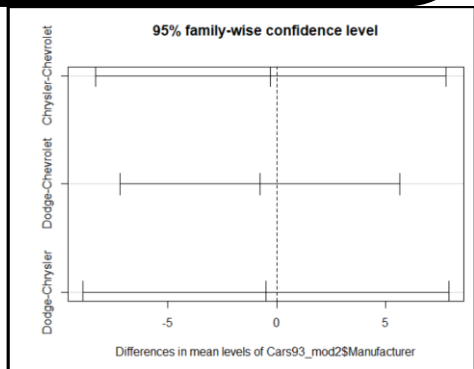
#4) Is the average highway MPG (MPG.highway) different across three car manufacturers (Manufacturer)?

#5) Is the average highway MPG (MPG.highway) different across four types of cars (Type)?

#6) Is the average number of insects (count) after spraying different across six types of spray (spray)?

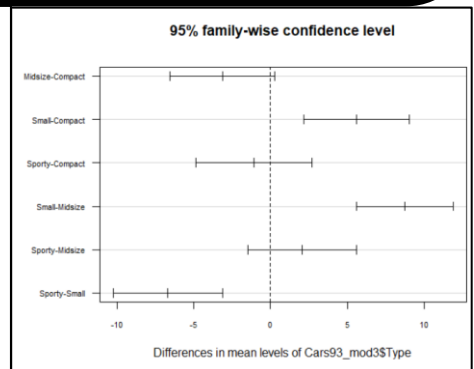
F = 0.052
p-value = 0.949

No, MPG is not different across the three manufacturers.



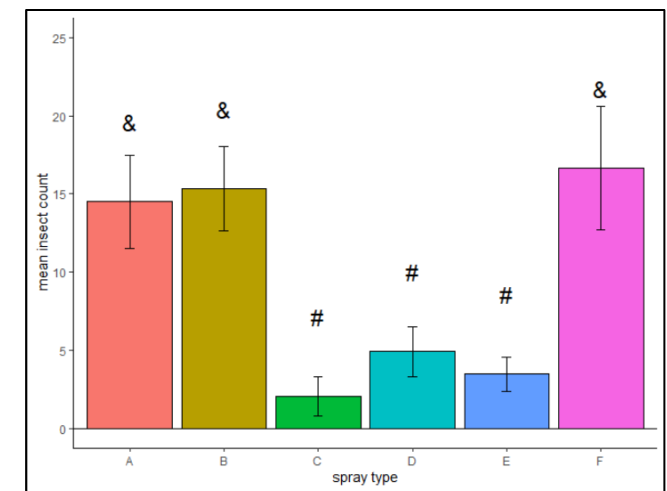
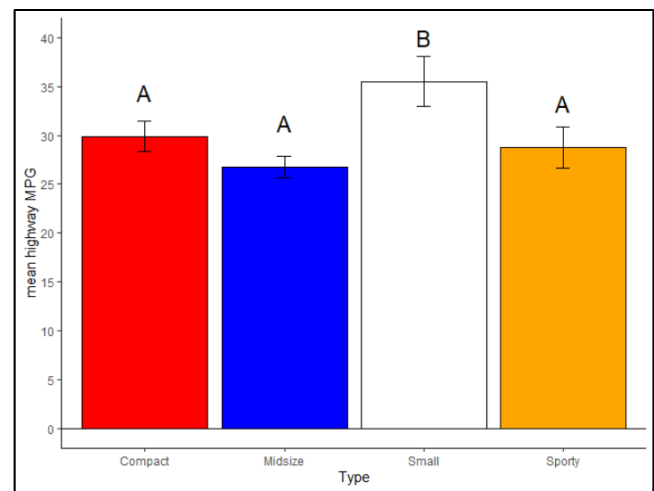
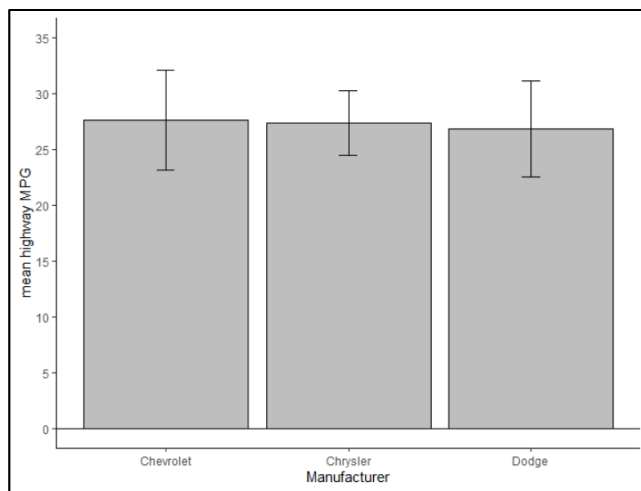
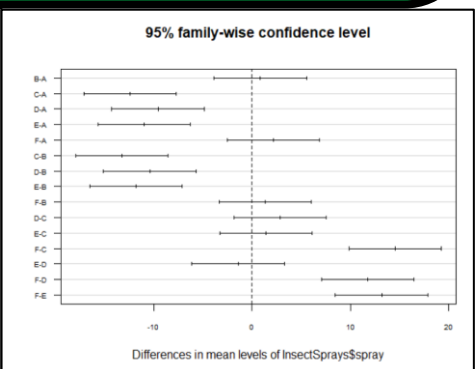
F = 18.99
p-value = 4.37e-09

Yes, Small cars had higher MPG than the other three types (Compact, Midsize, and Sporty).



F = 34.7
p-value = <2e-16

Yes, spray types C, D, and E, had lower insect counts after spraying than spray types A, B, and F.





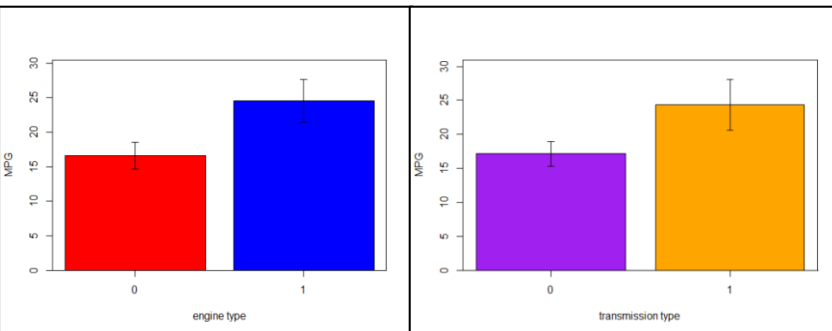
Two-way ANOVA

❖ *Tests if a variable's mean is different between two categories*

#1) Is the average miles per gallon (mpg) of 1975 Motor Trend vehicles different across the engine (vs) and transmission (am) type?

Variable	F-value	p-value
vs	41.20	5.98e-07
am	22.90	4.98e-05
vs:am	1.33	0.259

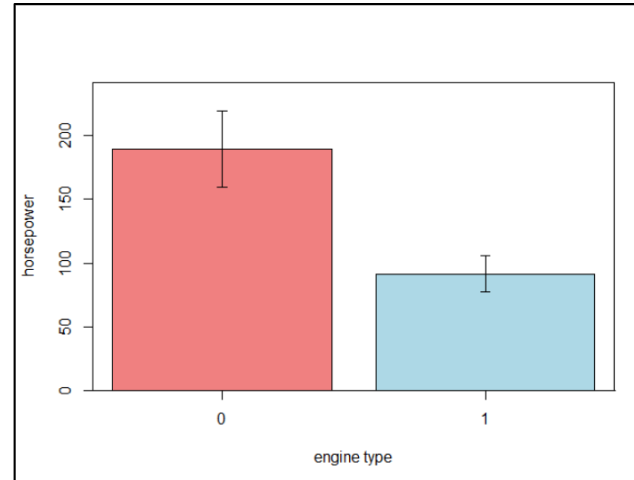
Yes, MPG was higher in cars with straight engines (1) and manual transmission (1), but the interaction was not significant.



#2) Is the average gross horsepower (hp) of 1975 Motor Trend vehicles different across the engine (vs) and transmission (am) type?

Variable	F-value	p-value
vs	31.75	4.91e-06
am	0.92	0.345
vs:am	0.05	0.820

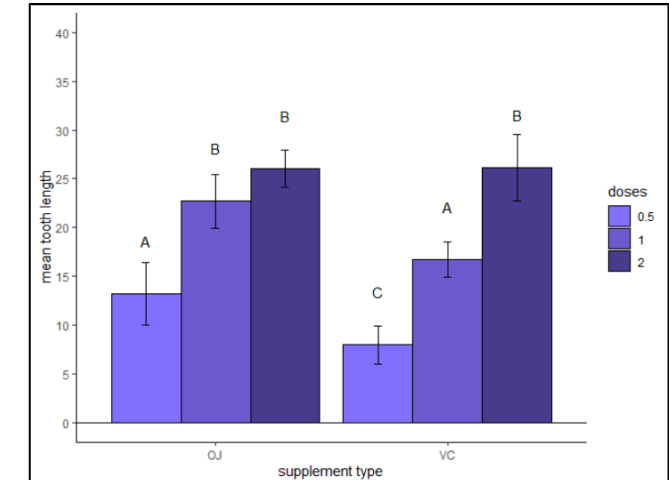
Yes, horsepower was higher in cars with v-shaped engines (0), but transmission and the interaction were not significant.



#3) Is the average tooth length of guinea pigs (len) different across supplement (supp) and dose (dose)?

Variable	F-value	p-value
supp	15.57	0.000231
dose	92.00	< 2e-16
supp:dose	4.11	0.021860

Yes, tooth length was significant across both variables and the interaction. Length increased with increasing dosage and differed between OJ and VC across dose categories.





Two-way ANOVA cont.

❖ *Tests if a variable's mean is different between two categories*

#4) Is the number of warp breaks per loom (breaks) different across wool (wool) and tension (tension)?

#5) Is the average yield for peas different across nitrogen (N) and phosphorus (P) application?

#6) Is the average price of diamonds different across cut (cut) and color (color)?

Variable	F-value	p-value
wool	3.77	0.058213
tension	8.50	0.000693
wool:tension	4.12	0.021044

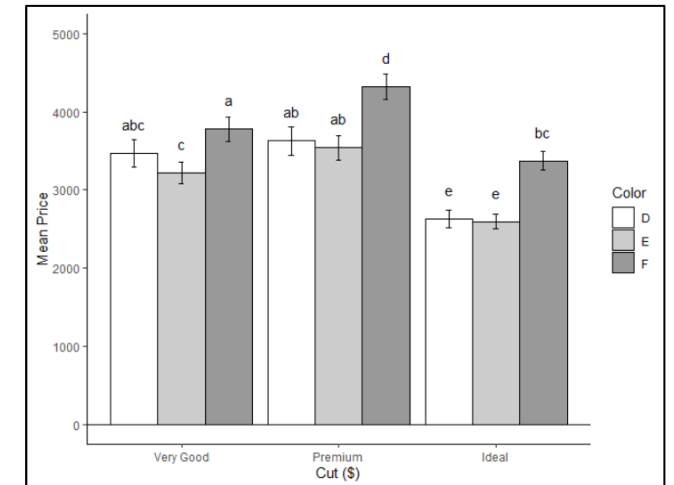
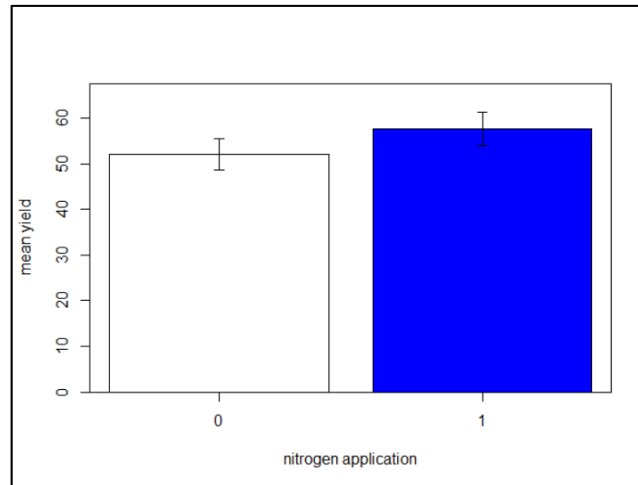
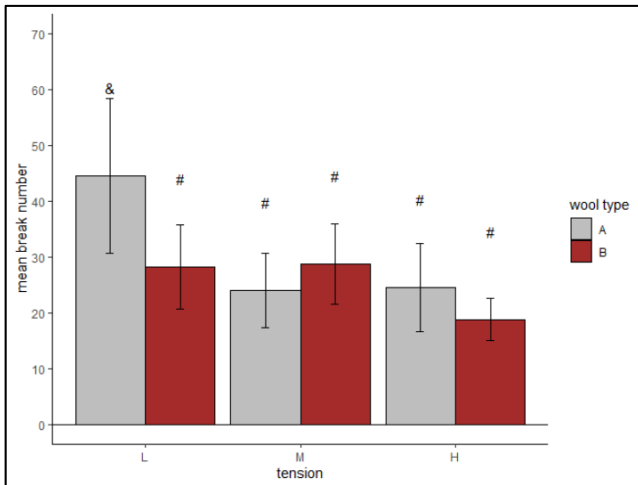
Yes, the number of warp breaks was significant across tension and the interaction. Type A wool on low tension (&) had higher breaks than the other groups (#).

Variable	F-value	p-value
N	5.76	0.0263
P	0.26	0.6187
N:P	0.65	0.4305

Yes, yield was higher in Nitrogen (N) plots, but Phosphorus (N) and the interaction were not significant.

Variable	F-value	p-value
cut	157.62	< 2e-16
color	100.41	< 2e-16
cut:color	2.42	0.0462

Yes, price was significant across cut, color, and interaction. Premium, F diamonds had a higher price than other groups, while ideal D-E diamonds lower prices than other groups.





Blocked/Nested ANOVA

❖ Tests if a variable's mean is different across categories while accounting for blocking/nesting

#1) Is the average yield (Y) of oats per sub-plot different across 3 varieties (V), while controlling for block (B)?

#2) Is the average yield for peas different across nitrogen (N) and potassium (K) application, while controlling for block?

#3) Is the decrease in honeybees (decrease) different across spray type (treatments), while controlling for row (rowpos) and column (colpos)?

Variable	F-value	p-value
V	1.67	0.197

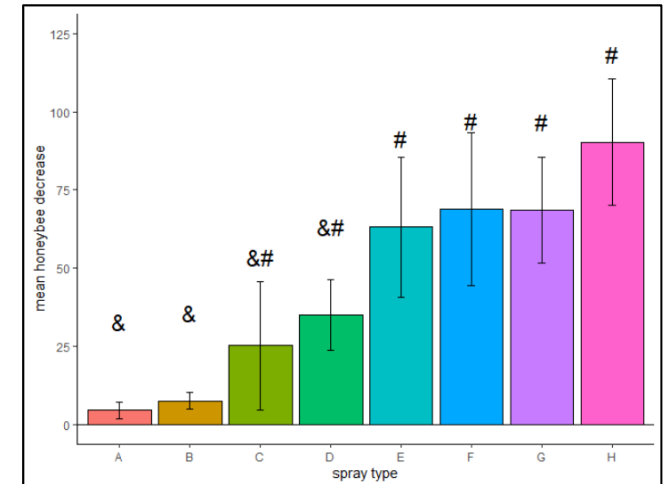
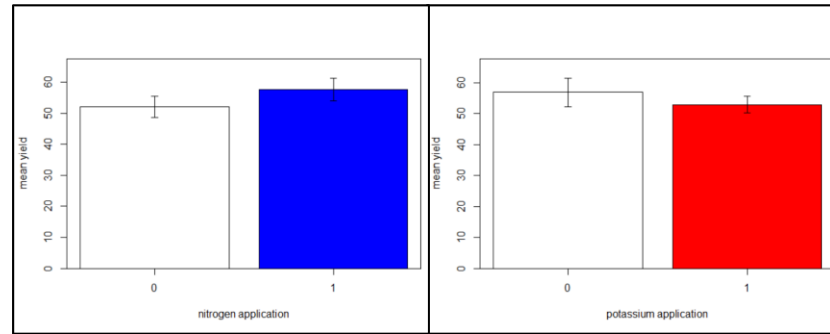
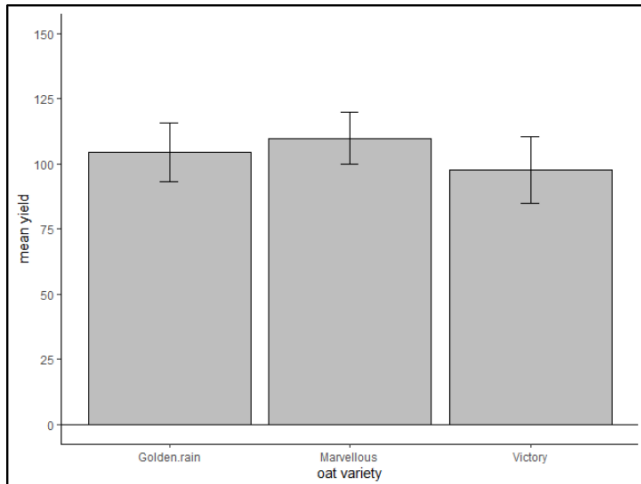
No, even after controlling for block, the average yield was not different across the three varieties.

Variable	F-value	p-value
N	13.18	0.00247
K	6.63	0.02114
N:K	2.31	0.14959

Yes, yield was higher in plots with nitrogen applied and with no potassium applied. The interaction was not significant even controlling for block.

Variable	F-value	p-value
Treatment	20.59	3.57e-13

Yes, the decrease in honeybees was lower in sprays A-B, while it was higher in sprays E-H, when controlling for row and column.





Blocked/Nested ANOVA cont.

❖ *Tests if a variable's mean is different across categories while accounting for blocking/nesting*

#4) Is the log-optical density (logDens) different across samples (samples) when nested in block (Block)?

Variable	F-value	p-value
sample	11.21	0.00952

No, while the overall model appeared significant using `aov()`, post hoc tests using results from using `lme()` found no differences in density across samples, even when nesting in block.

#5) Is the number of words recollected (Recall) different across word type (Valance) when nested in subject?

Variable	F-value	p-value
Valance	189.1	1.84e-07

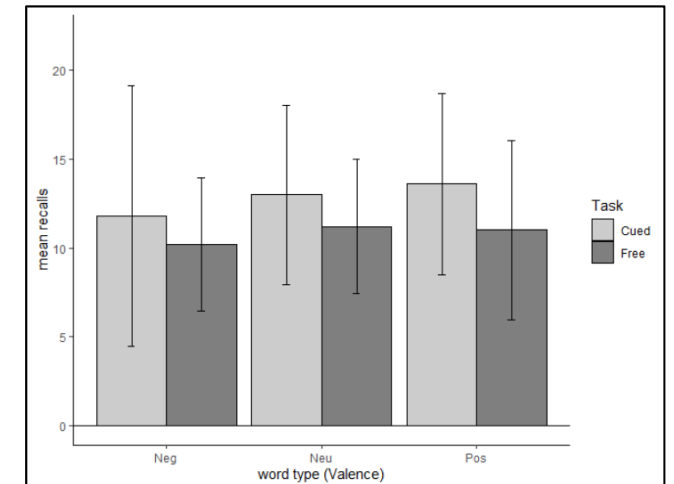
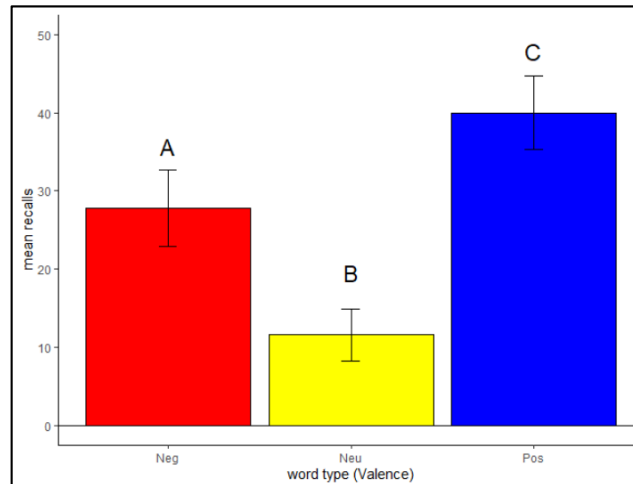
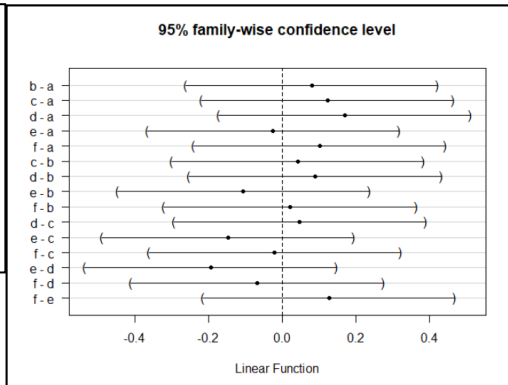
Yes, word recall was highest for positive words, lower for negative words, and the lowest for neutral words, when accounting for nesting in subject.

#6) Is the number of words recollected (Recall) different across word type (Valance) and (Task) when nested in subject?

Variable	F-value	p-value
Task	7.35	0.0535
Valance	1.46	0.288
Task:Valance	0.291	0.755

No, word recall was not different across task, valance, or the interacting, even when nesting in subject.

Comp.	t-value	p-value
A:B	0.67	0.5315
A:C	1.02	0.3536
A:D	1.42	0.2157
A:E	-0.21	0.8436
A:F	0.85	0.4347





Simple Linear Regression

❖ Tests if there is a relationship between a numerical response variable and one numerical predictor variable

#1) Is there a relationship between car speed (speed) and stopping distance (dist)?

#2) Is there a relationship between log animal brain weight (brain) and log body weight (body)?

#3) Is there a relationship between the area of pore space (area) and perimeter (peri) in petroleum rock samples?

Variable	Estimate	t-value	p-value
Intercept	8.28	9.47	1.44e-12
dist	0.17	9.46	1.49e-12

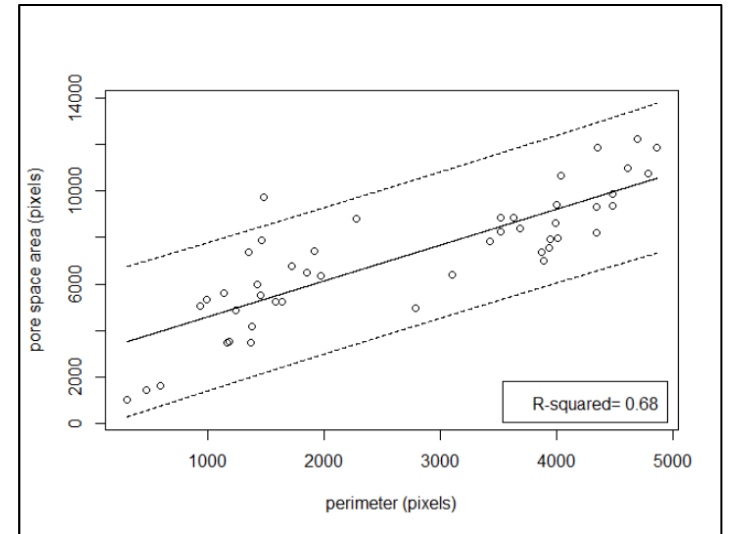
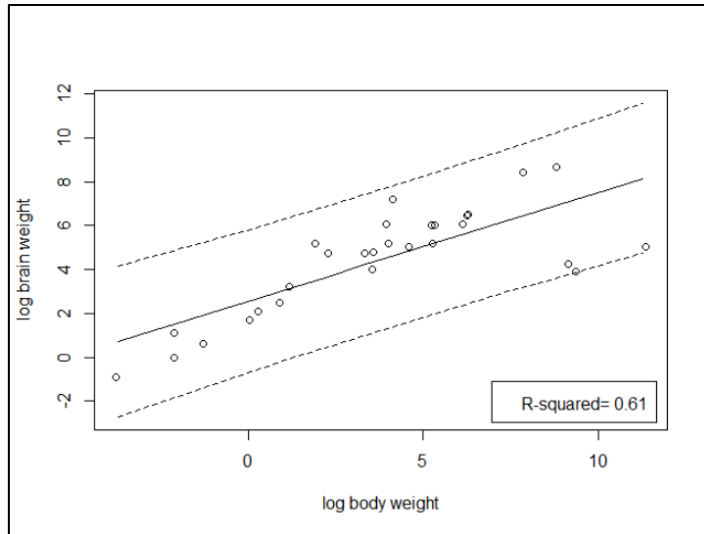
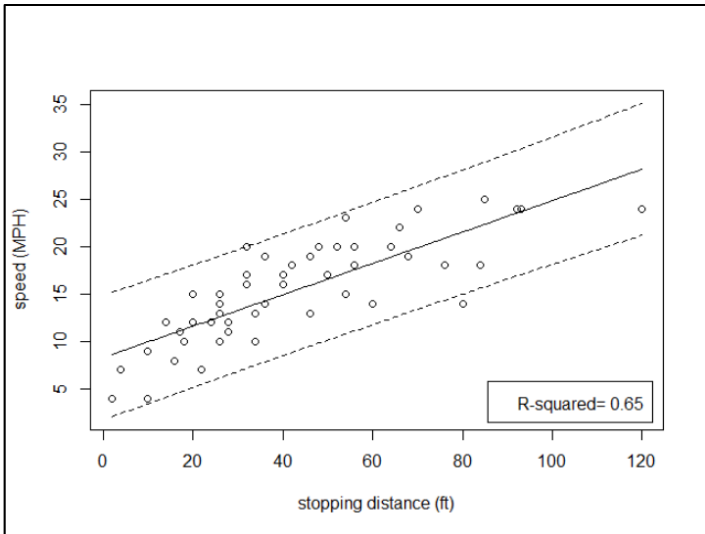
Yes, there was a positive relationship. Car speeds increased as stopping distance increased.

Variable	Estimate	t-value	p-value
Intercept	2.55	6.18	1.53e-06
log_body	0.50	6.35	1.02e-06

Yes, there was a positive relationship. Brain weight in animals increased as body weight increased.

Variable	Estimate	t-value	p-value
Intercept	3052.02	6.40	7.26e-08
peri	1.54	9.91	7.51e-13

Yes, there was a positive relationship. Pore space area in rocks increased as perimeter increased.





Simple Linear Regression cont.

❖ *Tests if there is a relationship between a numerical response variable and one numerical predictor variable*

#4) Is there a relationship between the area of pore space (area) and permeability (perm) in petroleum rock samples?

#5) Is there a relationship between fertility rates (Fertility) and the percent of education beyond primary school for draftees (Education) in Swiss provinces?

#6) Is there a relationship between infant mortality rates (Infant.Mortality) and the percent of males in agriculture (Agriculture) in Swiss provinces?

Variable	Estimate	t-value	p-value
Intercept	8197.86	16.46	<2e-16
perm	-2.43	-2.93	0.00525

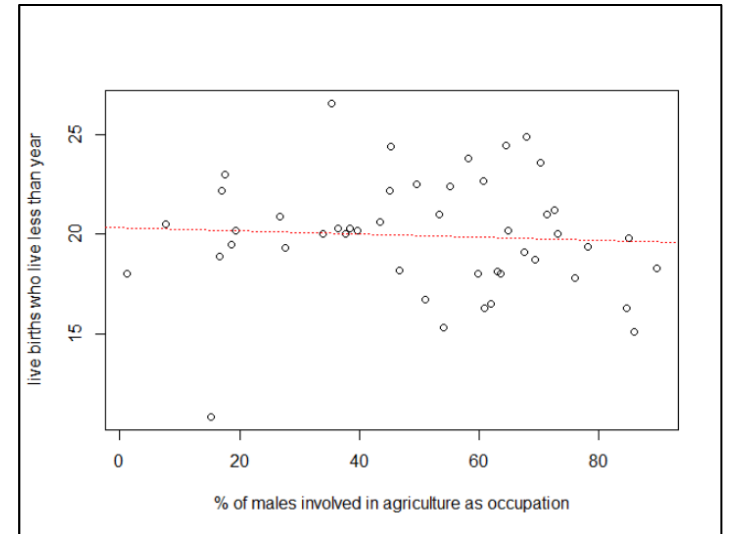
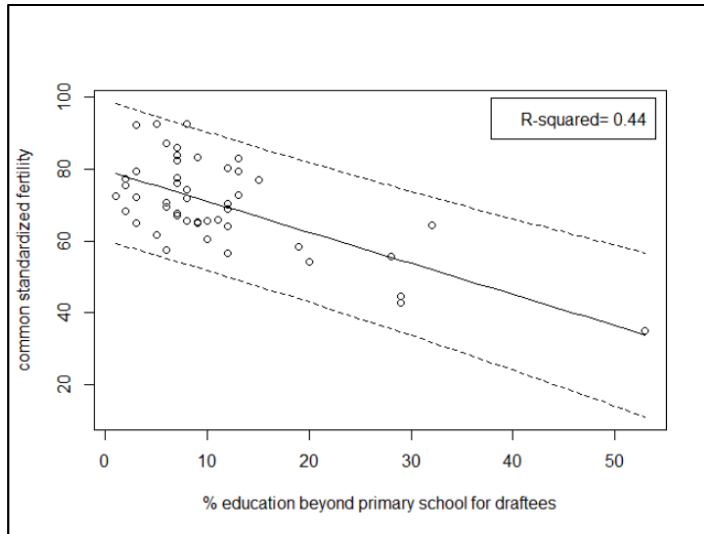
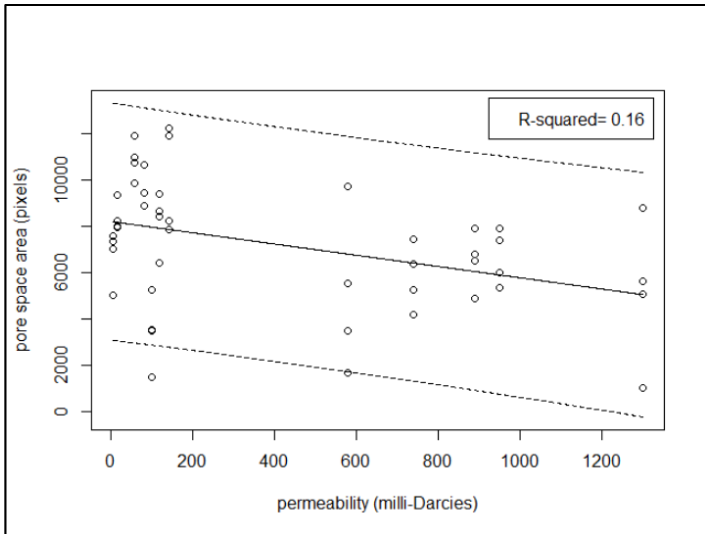
Yes, there was a negative relationship. Pore space area in rocks decreased as permeability increased.

Variable	Estimate	t-value	p-value
Intercept	79.61	37.84	< 2e-16
Education	-0.86	-5.95	3.66e-07

Yes, there was a negative relationship. Fertility rates in Swiss provinces decreased as education percentage increased.

Variable	Estimate	t-value	p-value
Intercept	20.34	19.23	<2e-16
Agriculture	-0.008	-0.41	0.684

No, there was no relationship between infant mortality rates and agriculture percentages in Swiss provinces.





Multiple Linear Regression

❖ Tests if there is a relationship between a numerical response variable and multiple numerical predictor variables

#1) Can the area of pore space (area) in petroleum rock samples be predicted by perimeter (peri) and permeability (perm)?

Variable	Estimate	t-value	p-value
Intercept	144.56	0.187	0.852
peri	2.19	11.10	1.81e-14
perm	2.85	4.42	6.14e-05

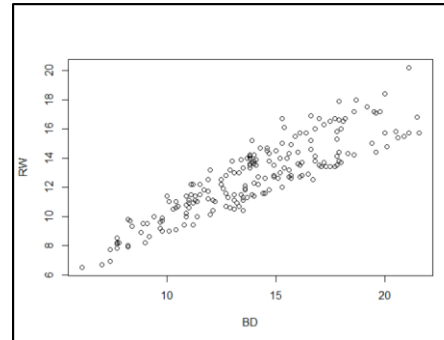
Model	AIC
peri only	844.96
perm only	890.91
peri + perm	829.64

Yes, both perimeter and permeability predicted area of pore space in rocks. The full model had the best fit. Pore space increased as perimeter and permeability increased.

#2) Can frontal lobe size (FL) in crabs be predicted by rear width (RW) and body depth (BD)?

Variable	Estimate	t-value	p-value
Intercept	1.44	8.77	8.15e-16
BD	1.01	88.62	< 2e-16

Model	AIC
RW only	727.24
BD only	332.09
RW + BD	298.98

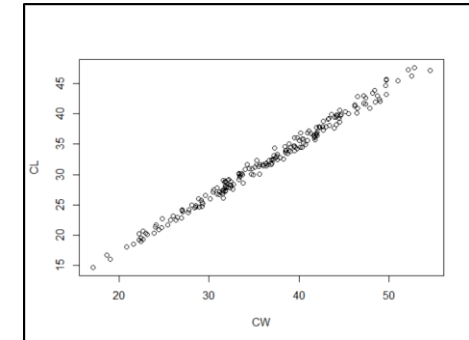


Yes, both rear width and body depth predicted frontal lobe size in crabs. The full model had the best fit, but since rear width and body depth were highly correlated, only the best fit single variable model (body depth) was retained. Frontal lobe size increased as body depth increased.

#3) Can frontal lobe size (FL) in crabs be predicted by carapace length (CL), width (CW), and their interaction?

Variable	Estimate	t-value	p-value
Intercept	0.15	0.65	0.52
CL	0.48	67.31	<2e-16

Model	AIC
CL only	438.50
CW only	538.01
CL * CW	398.90



Yes, both carapace length and carapace width predicted frontal lobe size in crabs. The full model had the best fit, but since carapace length and width were highly correlated, only the best fit single variable model (length) was retained. Frontal lobe size increased as carapace length increased.



Multiple Linear Regression cont.

❖ Tests if there is a relationship between a numerical response variable and multiple numerical predictor variables

#4) Can infant mortality rates (Infant.Mortality) in Swiss provinces be predicted by fertility rates (Fertility), % of males in agriculture (Agriculture), % Catholic (Catholic), and % education beyond primary school (Education)?

#5) Can calories per portion (calories) in US cereals be predicted by protein (protein), fat (fat), carbohydrates (carbo), or their interactions (sqrt-transformed data)?

#6) Can miles per gallon (mpg) be predicted by gross horsepower (hp), weight (wt), and quarter mile time (qsec), or their interactions?

Full Model

Variable	Estimate	t-value	p-value
Intercept	9.61	2.00	0.05188
Fertility	0.15	2.82	0.00722
Agriculture	-0.01	-0.56	0.59047
Catholic	-0.002	-0.19	0.84997
Education	0.07	0.95	0.34924

Simple Model

Variable	Estimate	t-value	p-value
Intercept	13.13	5.83	5.51e-07
Fertility	0.10	3.07	0.00359

Model	AIC
Full	231.89
Simple	229.91

Yes, fertility rate predicted infant mortality rates in Swiss provinces. The rest of the variables were not significant. The simple model (Fertility only) compared to the full model had a better fit, though by less than two. The full model could be retained to show the other variables' non-effect.

Model selection

Full Model: $\text{sqrt_calories} \sim \text{sqrt_protein} * \text{sqrt_fat} * \text{sqrt_carbo}$ (AIC=7.58)
 Final Model: $\text{sqrt_calories} \sim \text{sqrt_protein} + \text{sqrt_fat} + \text{sqrt_carbo} + \text{sqrt_protein}:\text{sqrt_carbo}$ (AIC=2.02)

Final Model

Variable	Estimate	t-value	p-value
Intercept	8.65	4.60	2.20e-05
Sqrt_protein	-1.69	-2.20	0.031374
Sqrt_fat	1.19	6.97	2.85e-09
Sqrt_carbo	0.06	0.13	0.896086
Sqrt_protein: sqrt_carbo	0.61	3.60	0.000644

Yes, after model selection and checking correlation of covariates, protein, fat, and the interaction of protein and carbohydrates predicted the calories per portion of US cereals. Calories decreased as protein increased, while calories increased as fat and the interaction term of protein and carbohydrates increased.

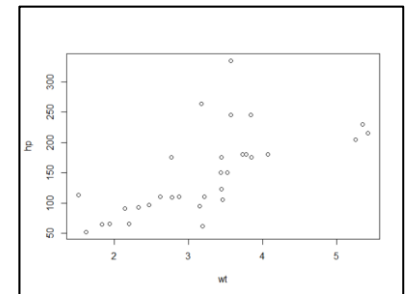
Model selection

Full Model: $\text{mpg} \sim \text{hp} * \text{wt} * \text{qsec}$ (AIC=56.83)
 Red. Model: $\text{mpg} \sim \text{hp} + \text{wt} + \text{qsec} + \text{hp}:\text{wt}$ (AIC=52.57)

Final Model

Variable	Estimate	t-value	p-value
Intercept	19.75	3.76	0.000765
wt	-5.05	-10.43	2.52e-11
qsec	0.93	3.51	0.001500

Model	AIC
hp * wt * qsec	149.64
hp + wt + qsec + hp:wt	145.38
wt + qsec	156.72



Yes, after model selection and removing horsepower because it was highly correlated with weight, weight and quarter mile time predicted miles per gallon for cars. MPG decreased as weight increased, while MPG increased as quarter mile time increased.



Logistic Regression

❖ *Tests if there is a relationship between a binary response variable and one or more predictor variables*

#1) Can midwest counties' metropolitan status (inmetro=Yes vs. No) be predicted by the log population density(log_popdensity)?

#2) Can midwest counties' metropolitan status (inmetro=Yes vs. No) be predicted by the percentage of college educated adults (percollege)?

#3) Can a car's origin (Origin2: USA vs. non-USA) be predicted by city miles per gallon (MPG.city)?

Variable	Estimate	z-value	p-value
Intercept	-21.81	-10.26	<2e-16
log_popdensity	2.88	10.03	<2e-16

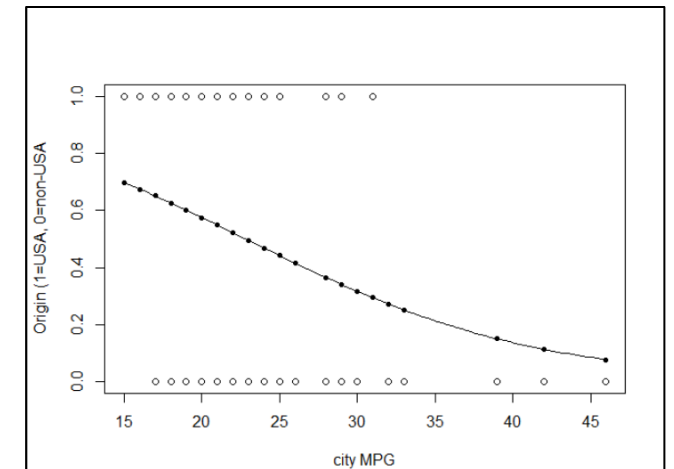
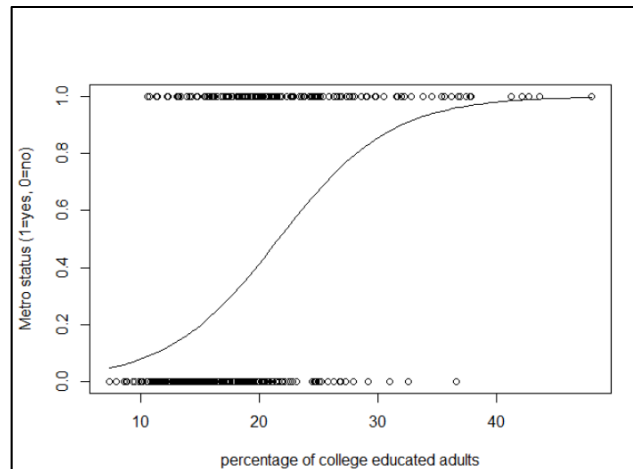
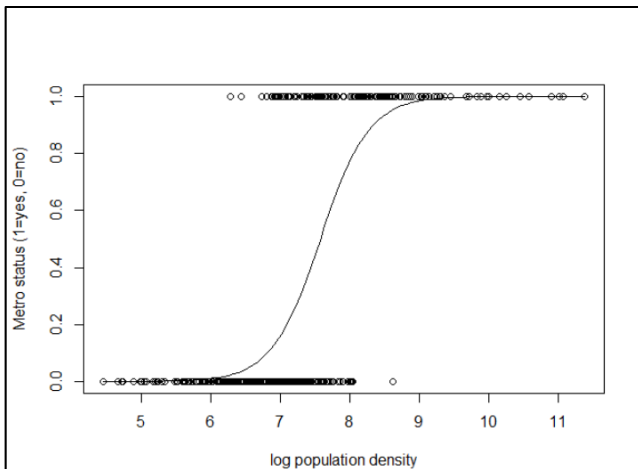
Variable	Estimate	z-value	p-value
Intercept	-4.56	-9.61	<2e-16
percollege	0.21	8.44	<2e-16

Variable	Estimate	z-value	p-value
Intercept	2.45	2.40	0.0165
MPG.city	-0.11	-2.36	0.0183

Yes, as the log population density increases, the probability of the county having a metropolitan status increases.

Yes, as the percentage of college educated adults increases, the probability of the county having a metropolitan status increases.

Yes, as city MPG increases, the probability that the car is of USA origin decreases.





Logistic Regression cont.

❖ Tests if there is a relationship between a binary response variable and one or more predictor variables

#4) Can a car's origin (Origin2: USA vs. non-USA) be predicted by midrange price (Price)?

Variable	Estimate	z-value	p-value
Intercept	0.48	1.00	0.316
Price	-0.02	-0.96	0.336

No, midrange price did not significantly predict origin status.

#5) Can the presence of a bacteria species (y: yes vs. no) in children be predicted by drug status (ap: placebo/active) and compliance (hilo: low/high)?

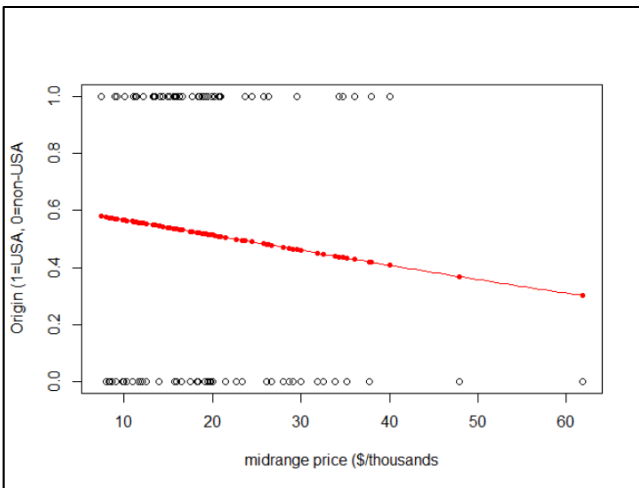
Variable	Estimate	z-value	p-value
Intercept	1.35	4.74	2.11e-06
spp	0.79	2.12	0.0343
hilolo	-0.48	-1.38	0.1664

Yes, drug status predicted the presence of bacteria in children, but compliance did not. Children with the placebo (app) were over twice as likely to have the bacteria compared to those with an active drug status (OR=2.21).

#6) Can the presence of a tumor (status: tumor vs. none) be predicted by sex (sex: male/female) and treatment (rex: control/drug)?

Variable	Estimate	z-value	p-value
Intercept	-1.38	-5.61	2.07e-08
rx	0.96	2.61	0.00909
sexm	-3.35	-4.54	5.71e-06

Yes, treatment and sex predicted the presence of tumors in rats. Rats given the treatment were over twice as likely to have a tumor compared to the control (OR=2.62), and male mice were much less likely to have a tumor compared to females (OR=0.035)



Odds Ratios (OR)

Variable	OR	2.5%	97.5%
app	2.21	1.08	4.76
hilolo	0.62	0.31	1.22

Odds Ratios (OR)

Variable	OR	2.5%	97.5%
rx	2.62	1.27	5.43
sexm	0.035	0.006	0.118

Acknowledgements

References

Title image: https://commons.wikimedia.org/wiki/File:Spießgasse_Frundsberger_Kriegsbuch_Jost_Ammann_1525.JPG

Examples 5 and 6 for Blocked/Nested ANOVA: <https://personality-project.org/r/r.guide/r.anova.html>

DaCCoTA

The DaCCoTA is supported by the National Institute of General Medical Sciences of the National Institutes of Health under Award Number U54GM128729. For projects that use the Biostatistics, Epidemiology, and Research Design Core in any way, including this presentation, please acknowledge us for publications. ***"Research reported in this publication was supported by DaCCoTA (the National Institute of General Medical Sciences of the National Institutes of Health under Award Number U54GM128729)".***

DaCCoTA
DAKOTA CANCER COLLABORATIVE
ON TRANSLATIONAL ACTIVITY